

## Rational Expressions Exactly Form Replacement

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**Abstract:** This article provides detailed theoretical examples and practical exercises about rational expressions and transformations on them.

**Keywords:** rational expressions, mathematical properties, theorems, natural numbers, etc.

Someone  $X(x_1, \dots, x_n)$  is algebraic expression *exactly replacement* that, him, in general when, to  $X$  unlike so  $Y(x_1, \dots, x_n)$  is algebraic to expression replacement it is understood that all  $x_1, \dots, x_n$  in values  $H$  values equal to let it be

For example,  $A(x) = \frac{(x^2 + 1)(x - 1)(x + 3)}{(x^2 - 1)(x + 3)}$ ,  $B(x) = \frac{x^2 + 1}{x + 1}$ ,  $C(x) = \frac{(x^2 + 1)(x - 1)(x + 3)}{(x^2 - 1)(x + 3)}$  expression

$A(x)$  from for all values  $x \neq -1, x \neq 1$ , expression  $B(x)$  for values  $x \neq -1$ , and  $C(x)$  for values  $x \neq 1, x \neq -1, x \neq -3$  determined. Their common availability area of values  $x \neq \pm 1, x \neq -3$  consists of, then they are one different values acceptance they do, that is, *exactly is equal*.

General availability in the field one rational expression to him exactly equal to replace with an expression that's it expression *exactly replacement* is called

Exactly of substitutions equations solution, theorems and crimes to prove such as issues in solving is used. Exactly substitutions fractions shortening, parentheses open, general a lot the stalker from parentheses out release, similar terms condense and that's it from the like consists of will be Exactly exchange in trouble arithmetic of deeds properties is used.

**The following crimes suitable for :**

$$1) (AB)^n = A^n B^n$$

$$2) A^m A^n = A^{m+n}$$

$$3) (A^m)^n = A^{mn}$$

$$4) \frac{A}{B} + \frac{C}{D} = \frac{AD + BC}{BD}, B \neq 0, D \neq 0.$$

$$5) \frac{A}{B} \cdot \frac{C}{D} = \frac{AC}{BD}, B \neq 0, D \neq 0.$$

$$6) \frac{A}{b} \div \frac{C}{D} = \frac{AD}{BC}, B \neq 0, C \neq 0, D \neq 0$$

$$7) \frac{AC}{BC} = \frac{A}{B}, B \neq 0, C \neq 0$$

$$8) \frac{A^m}{A^n} = \begin{cases} A^{m-n}, m > n \\ 1, m = n, A \neq 0 \end{cases} \text{ in};$$

9)  $|AB| = |A| \cdot |B|$

10)  $|A^n| = |A|^n$

Rational of expressions canonical shape irreducible  $\frac{P(x)}{Q(x)}$  from the fraction consists of will be Here  $P(x)$  and  $Q(x)$  are polynomials is , and  $Q(x)$  is a polynomial prime factor and  $x$  to 1 equal to

**Example 2:**  $\frac{16 - x^2}{2x^4 + 9} : \left( \frac{1}{x-3} - \frac{1}{x-3} * \frac{x-3}{2x+1} \right)$  rational expression canonical to look bring \_

**Solution :**  $\frac{1}{x-3} - \frac{1}{x-3} * \frac{x-3}{2x+1} = \frac{x+4}{(x-3)(2x+1)}$ ,

$$\frac{16 - x^2}{2x^4 + 9} : \left( \frac{x+4}{(x-3)(2x+1)} \right) = \frac{(4-x)(4+x)(x-3)(2x+1)}{(2x^4 + 9)(x+4)} = \frac{-2x^4 + 13x^2 - 17x - 12}{2x^4 + 9} = \frac{-x^3 + 13/2x^2 - 17/2x - 6}{x^4 + 9/2}$$

**2. Irrational expressions exactly form substitutions .**

*n*- level arithmetic root \_ Rational indicative degree \_

$a \geq 0$  is the *n*th power of the number **arithmetic root** as ( $n \in \mathbb{N}$ ), *n*- degree to  $a$  equal to to the number  $b \geq 0$  it is said and  $b = \sqrt[n]{a}$  through is determined . Description by :  $(\sqrt[n]{a})^n = a$  .

$a > 0$ ,  $m \in \mathbb{Z}$  and  $n \in \mathbb{N}$  if  $\sqrt[n]{a^m}$  number of  $a$   $r = \frac{m}{n}$  **rational indicative level** is called , that is,  $a^r = a^{\frac{m}{n}} = \sqrt[n]{a^m}$  .

In particular ,  $\sqrt[n]{a} = a^{\frac{1}{n}}$  . Rational indicative degree **characteristic s a 1 ar i** whole indicative degree properties similar \_  $a, b$  are optional positive numbers ,  $r$  and  $q$  are optional rational numbers let it be In that case :

1)  $(ab)^r = a^r b^r$  (1'). Indeed , let  $r = \frac{m}{n}$  ,  $n \in \mathbb{N}$  ,  $m \in \mathbb{Z}$  . In that case :

$$((ab)^r)^n = \left( (ab)^{\frac{m}{n}} \right)^n = \left( \sqrt[n]{(ab)^m} \right)^n = (ab)^m = a^m b^m = \left( \sqrt[n]{a^m} \right)^n \cdot \left( \sqrt[n]{b^m} \right)^n = \left( a^{\frac{m}{n}} \cdot b^{\frac{m}{n}} \right)^n = (a^r \cdot b^r)^n$$
 (1')

In particular ,  $\left( \frac{a}{b} \right)^r = \frac{a^r}{b^r}$  (2')

2)  $a^r \cdot a^q = a^{r+q}$  where  $r = \frac{k}{n}, q = \frac{m}{n}$ . (3') Indeed ,

$$\left( a^{\frac{k}{n}} \cdot a^{\frac{m}{n}} \right)^n = \left( a^{\frac{k}{n}} \right)^n \cdot \left( a^{\frac{m}{n}} \right)^n = \left( \sqrt[n]{a^k} \right)^n \cdot \left( \sqrt[n]{a^m} \right)^n = a^k \cdot a^m = a^{k+m} = \left( a^{\frac{k+m}{n}} \right)^n = \left( a^{\frac{k}{n} + \frac{m}{n}} \right)^n$$

3)  $\frac{a^r}{a^q} = a^{r-q}$  (4'). As in ((2'). is proved ). 4)  $(a^r)^q = a^{rq}$  , where  $r = \frac{p}{k}, q = \frac{m}{n}$ . (5') Indeed ,

$$\left( \left( \left( \frac{p}{a^k} \right)^m \right)^n \right)^{n-k} = \left( \left( \left( \left( \frac{p}{a^k} \right)^m \right)^n \right)^k \right) = \left( \left( \frac{p}{a^k} \right)^m \right)^k = (a^p)^m = \left( a^{\frac{pm}{kn}} \right)^{kn}$$

be

**Root** \_

Above arithmetic to the root definition given was  $a \geq 0$  at  $x = \sqrt[n]{a}$  number  $x^n = a$  of the equation the only one negative the solution that , and if  $a$  is  $\in \mathbb{R}$  and  $n$  is an odd natural number , then  $x^n = a$  of the equation the only one that it has a solution below is proved .

$x^n = a$  of the equation ( this where  $a \in \mathbb{R}, n \in \mathbb{N}$ ) each how root of the number a **n- level root** is called

**Theorem 1 .** *Har for any real number  $a \geq 0$  each always the equation  $x^n = a$  satisfactory there is a unique real number  $x \geq 0$  .*

**Theorem 2 a.** *If A is no natural number n- th power of a natural number if not ,  $\sqrt[n]{A}$  the number is irrational .*

**Proof .** Condition number of A on negative of numbers  $0^n, 1^n, 2^n, \dots, k^n, \dots$  . n- levels in sequence does not occur  $\sqrt[n]{A}$ , so not an integer . It is not even a fraction . Indeed ,  $\sqrt[n]{A} = \frac{p}{q}$  Let it be

let's say , where p and q are prime and  $p \neq 1, q \neq 0$ . Then  $A = \frac{p^n}{q^n} p^n$  and  $q^n$  is a reciprocal radical,  $q \neq 1$

number of A from being irreducible fraction will be And this condition opposite. Therefore ,  $\sqrt[n]{A}$  the number only is irrational . Theorem proof done \_

**Theorem 3 .** *If  $\frac{p}{q}, q \neq 1$ , is irreducible of the fraction photo and the denominator exactly nth degree if not ,  $\sqrt[n]{\frac{p}{q}}$  root irrational is a number .*

**Proof .** Conversely , the root assuming that it is a rational number let , i.e.  $\sqrt[n]{\frac{p}{q}} = \frac{a}{b}, B(a, b)=1$ . In that case  $\frac{p}{q} = \frac{a^n}{b^n}, B(a^n, b^n)=1$  and from which  $p = a^n, q = b^n$  to be come comes out. But a must on p and q n- degree not \_ So ,  $\sqrt[n]{\frac{p}{q}}$  is an irrational number. Proof done \_

**Theorem 4 a.** *Real numbers in the field odd level root only one valuable and his for this equality suitable for :*

$${}^{2n+1}\sqrt{-a} = -{}^{2n+1}\sqrt{a}$$

**I Proof.**  $x^{2n+1} = a, a \geq 0$ , equation (1).  $\forall a \in \mathbb{R}$  the only one that it has a solution we show :

a) Let  $a \geq 0$  without  $\forall x^{2n+1} < 0$  for the number  $x < 0 \leq a$ . So , the existence of (1) is from Theorem 1 visible ,  $x = {}^{2n+1}\sqrt{-a} \geq 0$  root his the only one real is the root ;

if  $a < 0$ , (1) in the form  $(-x)^{2n+1} = -a$  writing get it is possible that  $-a > 0$  for,  $a$ ) to the case according to the last equation and, therefore, equation (1) is also unique  $x = \sqrt[2n+1]{-a}$  to the solution has \_

$\forall a \in \mathbb{R}$  for  $x_1 = \sqrt[2n+1]{-a}$  and  $x_2 = \sqrt[2n+1]{-a}$  numbers (1) of roots will be. Above proven - to according to,  $x_1 = x_2$ . Theorem proof done \_

From the theorem it seems that,  $\sqrt[n]{a^n} = a$  is always greater than 1 of  $n$  in odd natural values, for arbitrary  $a \in \mathbb{R}$  appropriate. If  $n = 2m$  (this where  $m \in \mathbb{N}$ ),  $\sqrt[2m]{a^{2m}} = \sqrt[2m]{|a|^{2m}} = |a|$  will be. So, if  $a \geq 0$ ,  $\sqrt[2m]{a^{2m}} = a$  is equality, when  $a < 0$  while  $\sqrt[2m]{a^{2m}} = -a$  equality appropriate.

**Example 3.**  $\sqrt{(-7)^2} = \sqrt{|-7|^2} = |-7| = 7, \dots \sqrt{(-7)^2} = \sqrt{49} = 7.$

If  $a \leq 0, b \leq 0$ , then  $ab \geq 0$  and  $\sqrt{ab} = \sqrt{|a||b|} = \sqrt{|a|}\sqrt{|b|}$  will be

**Example 4.**  $\sqrt{(-3)(-12)} = \sqrt{|-3||-12|} = \sqrt{36} = 6.$

### 3. Arithmetic the roots form replacement \_

Multiplication to the  $n$ th degree root multipliers are of  $n$ - degree of the roots to the product equal :  $\sqrt[n]{a \cdot b \cdot \dots \cdot c} = \sqrt[n]{a} \cdot \sqrt[n]{b} \cdot \dots \cdot \sqrt[n]{c}$ , (1) this where  $a \geq 0, b \geq 0, \dots, c \geq 0$ .

Indeed,  $\sqrt[n]{a \cdot b \cdot \dots \cdot c} = (a \cdot b \cdot \dots \cdot c)^{\frac{1}{n}} = a^{\frac{1}{n}} \cdot b^{\frac{1}{n}} \cdot \dots \cdot c^{\frac{1}{n}} = \sqrt[n]{a} \cdot \sqrt[n]{b} \cdot \dots \cdot \sqrt[n]{c}.$  (2)

In particular,  $\sqrt[n]{a^n b} = \begin{cases} |a|^n \sqrt[n]{b}, \text{ agar } n - \text{juft } bo'lsa, \\ a^n \sqrt[n]{b}, \text{ agar } n - \text{toq } bo'lsa. \end{cases}$

Multiplier root hint under input : ,  $a \sqrt[n]{b} = \sqrt[n]{a^n b}$  ( $a > 0, b > 0$ ). (3)

From the palace root output :  $\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}$ , ( $a \geq 0, b \geq 0$ ). (4)

The root to the degree raise for root under expression that's it to the degree raise enough :

$(\sqrt[n]{a})^m = \sqrt[n]{a^m}$ , ( $a \geq 0$ ). (5)

Indeed,  $(\sqrt[n]{a})^m = \left(a^{\frac{1}{n}}\right)^m = a^{\frac{m}{n}} = (a^m)^{\frac{1}{n}} = \sqrt[n]{a^m}.$

$a$  is the  $n$ -th degree of the  $m$ -th degree of the number root to find for  $n$ - degree of a root to the  $m$ -th degree raise is enough, i.e.  $\sqrt[n]{a^m} = (\sqrt[n]{a})^m$ , ( $a > 0$ ). (6)

From the root release for root under expression unchanged are left, the roots indicators while is multiplied :  $\sqrt[n]{\sqrt[m]{a}} = \sqrt[n \cdot m]{a}$  ( $a \geq 0$ ). (7)

Indeed,  $\sqrt[n]{\sqrt[m]{a}} = \left(a^{\frac{1}{m}}\right)^{\frac{1}{n}} = a^{\frac{1}{m \cdot n}} = a^{\frac{1}{n \cdot m}} = \sqrt[n \cdot m]{a}.$

#### 4. Irrational expressions simplification.

Numbers, letters and algebraic operations ( adding , subtracting , multiplying, dividing , to the degree raise and root output ) is compiled with expression *algebraic expression* is called

Root release practice attended expression that's it to the argument relatively *irrational expression* is called

For example,  $3 - \sqrt{5}, \sqrt{5 + \sqrt{a}}, \sqrt{a^2 - \sqrt{ab}}$  expressions irrational are expressions .

Irrational expressions on deeds arithmetic deeds laws and roots on action to the rules according to will be done .

**Example 6 .** Level root from underneath in release degree indicator root to the indicator is divided . Out division and residual suitable in order root from underneath came out and root under the rest don't count degree indicators gives ,  $\sqrt[5]{a^7 b^9 c^{-10}} = abc^{-2} \sqrt[5]{a^2 b^4}$  .

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